

# AN ABSTRACTION FOR THE ANALYSIS OF SECURE POLICY INTEROPERABILITY

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# POLICY-BASED MANAGEMENT BASICS

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Policies are sets of rules governing the behaviour of a system. They are often used as a means of implementing flexible and adaptive systems for the management of Internet services, distributed systems, and security systems.

- Permissions

`permission(p1,subject,action,object,context)`

- Prohibitions

`prohibition(p2,subject,action,object,context)`

- Obligations

`obligation(p1,subject,action,object,activation_context,violation_context)`

“

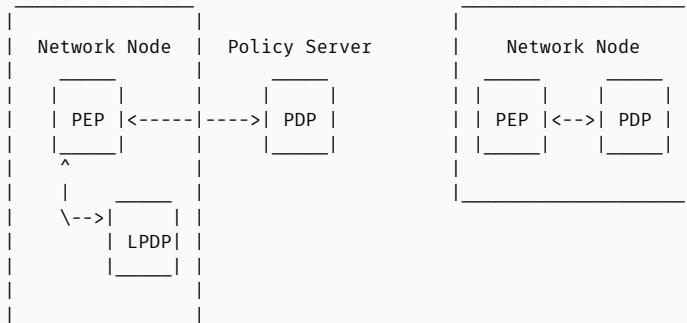


Figure 2: Two other possible configurations of policy control architecture components. The configuration on the left shows a local decision point at a network node and the configuration on the right shows PEP and PDP co-located at the same node.

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Rule1: All users are forbidden to reboot virtual servers.

Rule2: System administrators are authorised to manage any virtual device.

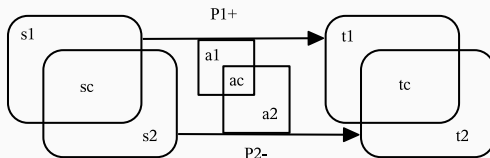


Figure 1: Overlapping Subjects, Objects and Actions (source [5]).

**“Policy conflict:** Occurs when the actions of two rules (that are both satisfied simultaneously) contradict each other. The entity implementing the policy would not be able to determine which action to perform. The implementers of policy systems must provide conflict detection and avoidance or resolution mechanisms to prevent this situation. *‘Policy conflict’* is contrasted with *‘policy error’*.”

[RFC 3198]

# HOW POLICY BASED SYSTEMS MANAGE CONFLICTS?

**Negative policies always have priority.** A forbidden action will never be permitted.

**Assigning explicit priorities.** An administrator assigns explicit priority-values to policies in order to define a precedence ordering.

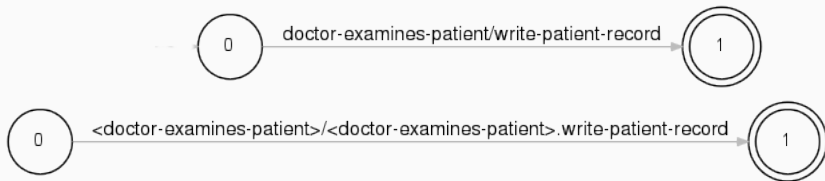
**Distance between a policy and the managed objects.** Priority is given to the policy applying to the closest class in the inheritance hierarchy when evaluating access to an object referenced in a query.

# FSTs FOR POLICY MODELLING

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Rule3: Every time a client asks for a virtualized web-server, he or she has to provide a domain name registration.



**Figure 2:** Two possible correspondences between Rule 3's constituents and FST elements.

Rule4: When a health professional examines a patient, she/he must write notes in the patient's medical record.

Rule5: When a mental health professional examines a patient, notes must be recorded in a place other than the patient's medical record.

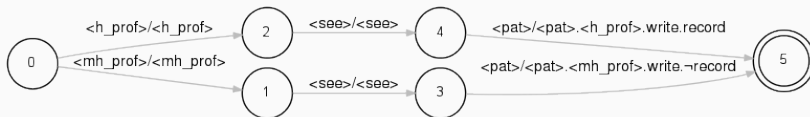


Figure 3: The Union of FSTs modelling rules 6 and 7.

## A LITTLE BACKGROUND ON FINITE STATE TRANSDUCERS

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A **semiring**  $(\mathbb{K}, \oplus, \otimes, \bar{0}, \bar{1})$  is a **ring** that may have no additive inverse.  
Thus for any  $a, b, c \in \mathbb{K}$ :

$$a \oplus b = b \oplus a$$

$$a \oplus (b \oplus c) = (a \oplus b) \oplus c$$

$$a \oplus 0 = a$$

$$a \otimes (b \otimes c) = (a \otimes b) \otimes c$$

$$a \otimes 0 = 0 \otimes a = 0$$

$$a \otimes 1 = 1 \otimes a = a$$

$$a \otimes (b \oplus c) = a \otimes b \oplus a \otimes c$$

$$(a \oplus b) \otimes c = a \otimes c \oplus b \otimes c$$

Closed semirings which are semirings with an additional operation called closure ( $*$ ) which satisfies:

$$a^* = 1 \oplus a \otimes a^* = 1 \oplus a^* \otimes a$$

If we have an affine map  $x \mapsto ax + b$  in some closed semiring, then  $x = a^*b$  is a fixpoint, since  $a^*b = (aa^* + 1)b = a(a^*b) + b$ .

The regular languages form a closed semiring where  $\otimes$  is concatenation,  $\oplus$  is union, and  $*$  is the Kleene star. Here the infinite geometric series interpretation of  $*$  is the most natural:  $a^*$  is the union of  $a^n$  for all  $n$ .

Other semirings:

Semiring	Set	$\oplus$	$\otimes$	$\bar{0}$	$\bar{1}$
Boolean	$\{0, 1\}$	$\vee$	$\wedge$	0	1
Probability	$\mathbb{R}_+$	$+$	$\times$	0	1
Tropical	$\mathbb{R}_+ \cup \{-\infty, +\infty\}$	$\min$	$+$	$+\infty$	0
String	$\Sigma^* \cup \{\infty\}$	$\wedge$	$\cdot$	$\infty$	$\epsilon$

For strings,  $\wedge$  is longest common prefix.

$(S, \oplus, \otimes, 0, 1)$  : a semiring

$(\mathbb{M}_n, \oplus, \otimes, J, I)$  : the semiring of  $n \times n$ -matrices over  $S$

$$(A \oplus B)(i, j) = A(i, j) \oplus B(i, j)$$

$$(A \otimes B)(i, j) = \bigoplus_{1 \leq q \leq n} A(i, q) \otimes B(q, j)$$

$$J(i, j) = 0$$

$$I(i, j) = \begin{cases} 1 & \text{if } i = j \\ 0 & \text{otherwise} \end{cases}$$

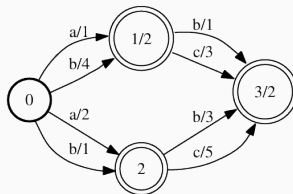


Figure 4: A FST with weights (source [6]).

Probability semiring ( $\mathbb{R}_+, +, \times, 0, 1$ )	Tropical semiring ( $\mathbb{R}_+ \cup \{-\infty, +\infty\}, \min, +, +\infty, 0$ )
$\llbracket A \rrbracket(ab) = 14$	$\llbracket A \rrbracket(ab) = 4$
$(1 \times 1 \times 2 + 2 \times 3 \times 2 = 14)$	$(\min(1 + 1 + 2, 3 + 2 + 2) = 4)$



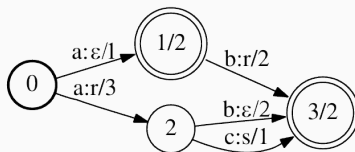


Figure 5: A FST with weights (source [6]).

Probability semiring $(\mathbb{R}_+, +, \times, 0, 1)$	Tropical semiring $(\mathbb{R}_+ \cup \{-\infty, +\infty\}, \min, +, +\infty, 0)$
$\llbracket T \rrbracket(ab, r) = 16$ $(1 \times 2 \times 2 + 3 \times 2 \times 2 = 16)$	$\llbracket T \rrbracket(ab, r) = 5$ $(\min(1 + 2 + 2, 3 + 2 + 2) = 5)$

Alphabets: input  $\Sigma$ , output  $\Delta$ . States:  $Q$ , initial states  $I$ , final states  $F$ .  
Transitions:  $E \subseteq Q \times (\Sigma \cup \{Q\}) \times (\Delta \cup \{Q\}) \times \mathbb{K} \times Q$ . Weight functions:  
initial weight function  $\lambda : I \rightarrow \mathbb{K}$  final weight function  $\rho : F \rightarrow \mathbb{K}$

**Automaton**  $A = (\Sigma, Q, I, F, E, \lambda, \rho)$  with for all  $x \in \Sigma^*$  :

$$\llbracket A \rrbracket(x) = \bigoplus_{\pi \in P(I, x, F)} \lambda(p[\pi]) \otimes \omega[\pi] \otimes \rho(n[\pi])$$

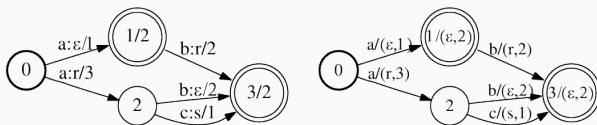
**Transducer**  $T = (\Sigma, \Delta, Q, I, F, E, \lambda, \rho)$  with for all  $x \in \Sigma^*, y \in \Delta$  :

$$\llbracket T \rrbracket(x, y) = \bigoplus_{\pi \in P(I, x, y, F)} \lambda(p[\pi]) \otimes \omega[\pi] \otimes \rho(n[\pi])$$

# TRANSDUCERS AS WEIGHTED AUTOMATA

A transducer  $T$  is **deterministic** (or *functional*) iff for each  $x$  there exists at most one  $y$  such that  $\llbracket T \rrbracket(x, y) = 0$

- An unweighted functional transducer can be seen as a weighted automata over the string semiring  $(\Sigma^* \cup \{\infty\}, \wedge, \cdot, \infty, \epsilon)$ .
- A weighted functional transducer over the semiring  $K$  can be seen as a weighted automata over the cartesian product of the *string semiring* and  $\mathbb{K}$ .



**Figure 6:**  $\llbracket T \rrbracket(ab, r) = 5$ ,  $\llbracket A \rrbracket(ab) = (r, 5)$  on a Tropical semiring  $(\mathbb{R}_+ \cup \{-\infty, +\infty\}, \min, +, +\infty, 0)$  (source [6]).

# OPERATIONS: SUM (UNION)

$$\llbracket T_1 \oplus T_2 \rrbracket(x, y) = \llbracket T_1 \rrbracket(x, y) \oplus \llbracket T_2 \rrbracket(x, y)$$

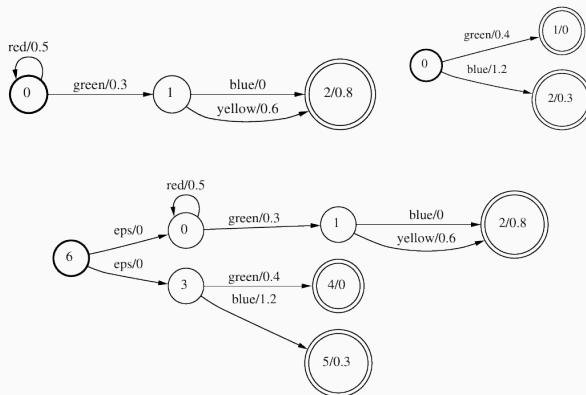


Figure 7: A Union of Weighted FSTs (source [6]).

$$\llbracket T \rrbracket(x, y) = \bigoplus_{n=0}^{\infty} \llbracket T^n \rrbracket(x, y)$$

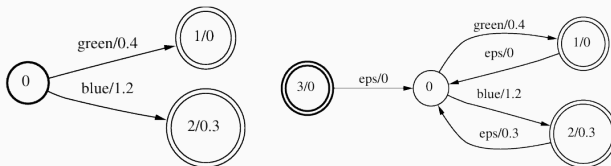


Figure 8:  $T$  and  $T^*$  (source [6]).

# OPERATIONS: COMPOSITION

$$\llbracket T_1 \circ T_2 \rrbracket(x, y) = \bigoplus_z \llbracket T_1 \rrbracket(x, z) \otimes \llbracket T_2 \rrbracket(z, y)$$

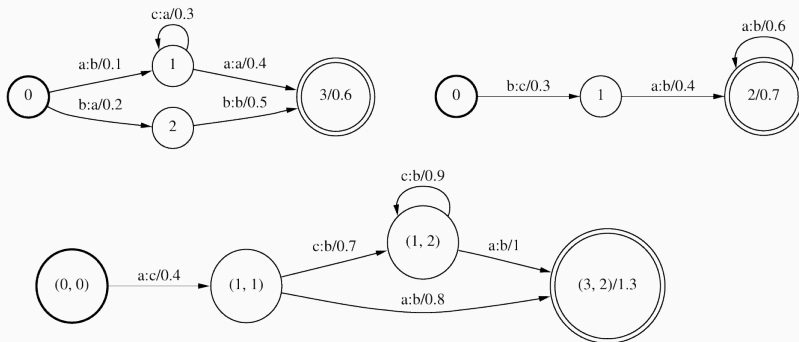


Figure 9:  $T_1$ ,  $T_2$ , and  $T_1 \circ T_2$  (source [6]).

Actually it is a **matrix multiplication!**

# OPERATIONS: (ACCEPTOR'S) INTERSECTION

$$\llbracket A_1 \cap A_2 \rrbracket(x) = \llbracket A_1 \rrbracket(x) \otimes \llbracket A_2 \rrbracket(x)$$

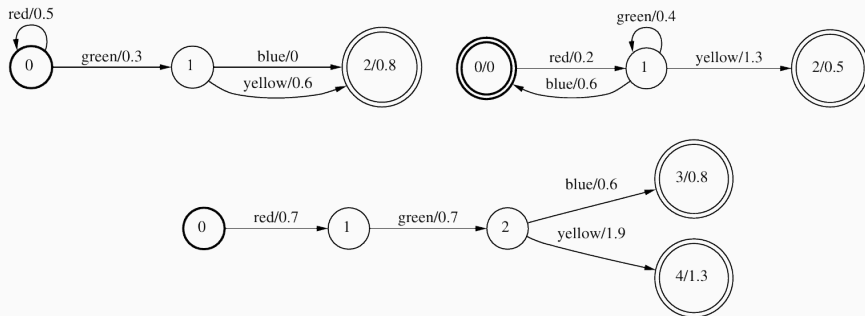
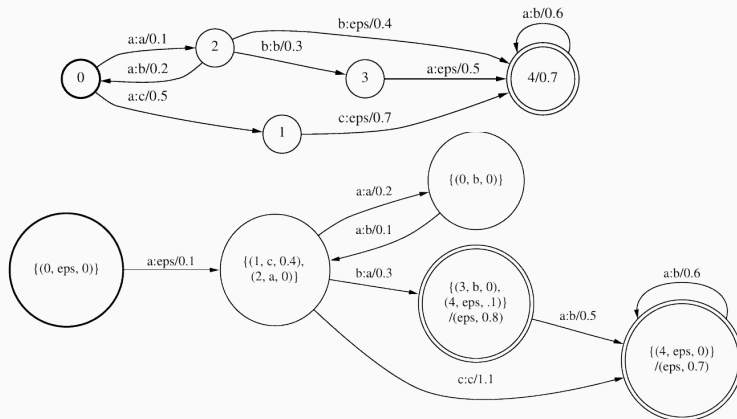


Figure 10:  $A_1$ ,  $A_2$ , and  $A_1 \cap A_2$  (source [6]).

# DETERMINIZATION OF WEIGHTED TRANSUCERS

An acceptor is deterministic iff for each state  $q$  there is at most one transition labeled with a given label. A transducer can be input deterministic (or subsequential) or output deterministic.





If  $M(i, j)$  is the adjacency matrix of a graph, then

$M^k(i, j)$  is the length of the shortest path with  $k$  edges from node  $i$  to node  $j$ , and

$M^*$  is the sum (which in the tropical semiring means “minimum”) of  $M^k$  for any  $k$ . Thus,

$M^*(i, j)$  is the length of the shortest path with any number of edges from node  $i$  to node  $j$ .

## WRITING RULES AS FSTs

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A FST  $T$  over a semiring  $(\mathbb{K}, \oplus, \otimes, \bar{0}, \bar{1})$  is a tuple  $(Q, E, P, \Pi, S, F, \lambda, \rho)$  where:

$Q$  is a finite set of states,

$E$  is a set of symbols,

$P$  is a set of predicates over  $E$ .

$\Pi$  is a finite set of transitions

$Q \times (P \cup \{\epsilon\}) \times \mathbb{K} \times (P \cup \{\epsilon\}) \times \mathbb{K} \times Q \times \{-1, 0, 1\}$ .<sup>1</sup>  $S \subseteq Q$  is a set of start states,  $F \subseteq Q$  is a set of final states,  $\lambda$  is an initial weight and  $\rho$  a final weight function. For all transitions  $(p, d, u, r, w, q, 1)$  it must be the case that  $d = r \neq \epsilon$ .

$\hat{\Pi} \subseteq Q \times E^* \times E^* \times Q$  is the relation defined by  $T$ .

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<sup>1</sup>The final component of a transition is a sort of “identity flag” used to indicate when an incoming event must be replicated in the output.

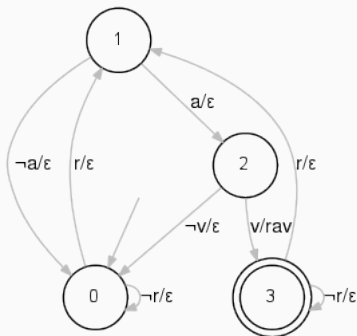
In the context of a system in which everything is prohibited by default, the OrBAC rule

`permission(p1,r,a,v,true)`

is modelled as the following FST:

$$T_{p+} = \left( id(R_p)^* \varepsilon(\overline{E^* R_p E^*})^* \right)^*$$

where  $R_p$  is the FSR that consumes exactly the event string  $rav$ ,  $id(X)$  is the identity FST,  $\varepsilon(X)$  is a transducer that consumes language  $X$  and produces  $\epsilon$  always,  $*$  is the *Kleene* closure, and  $E^*$  is the language of all possible strings of events.



**Figure 11:** An FST modeling a permission (weights are not included because they have no role at this stage).

In the context of a system that permits everything by default, the FST that models the rule

`prohibition(p1,r,a,v,TRUE)`

is the following:

$$T_{p-} = \left( \varepsilon (R_p)^* id (\overline{E^* R_p E^*})^* \right)^*$$

## PROHIBITIONS (CONT'D)

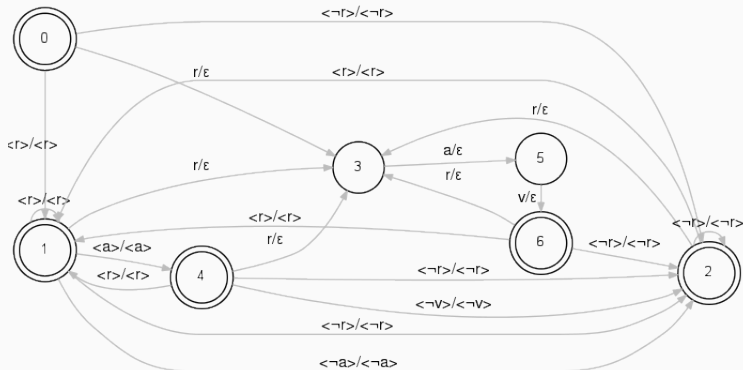


Figure 12: An FST Modeling a Prohibition.

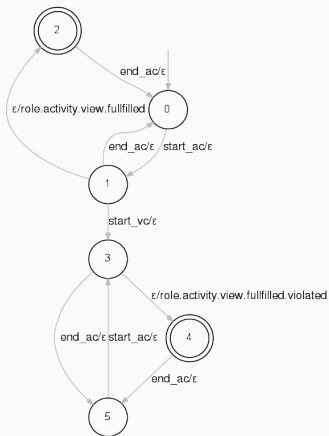


Figure 13: The obligation  $\text{obligation}(p1, r, a, v, ac, vc)$ .



Rule6: When a health professional examines a patient, she/he must write notes in the patient's medical record.

Rule7: When a mental health professional examines a patient, notes must be recorded in a place other than the patient's medical record.

A transducer is *sequential* when, standing in any state and consuming any possible input symbol, there is only one edge with a matching input label. A transducer is *determinist* when it produces at most one output string for each possible input string.

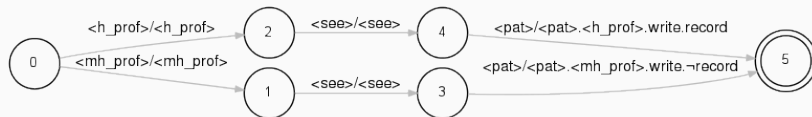


Figure 14: The Union of FSTs modelling rules 6 and 7.

This transducer is neither sequential, nor deterministic.

# POLICY CONFLICT RESOLUTION III

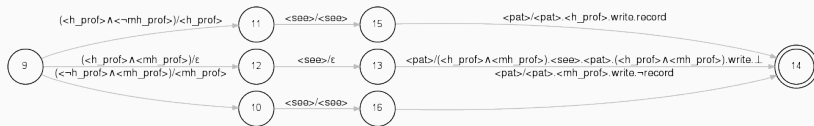


Figure 15: Previous FST determinized.

- Once we have a policy transducer  $T$ , it is possible to compute the shortest path on the Cartesian product of the semiring  $\{0,1\} \times \mathbb{R}^+ \times \{0,1\} \times \mathbb{R}^+$  computing the closure  $T^*$ .
- Submodules can be used to model action contradictions and remove them from the valid paths.

# INTEROPERABILITY ANALYSIS

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**Interoperability:** “The capability to communicate, execute programs, or transfer data among various functional units in a manner that requires the user to have little or no knowledge of the unique characteristics of those units” [3]

**What we do analyze when we analyze Interoperability?**

1. what is permitted if we apply the security rules of two organizations at the same time?
2. are the obligated actions consistent between them and with the prohibitions of both organizations?
3. is the emerging policy in line with their cooperation objectives?

- subjects, objects and actions at different organizations may have different names, classifications, and meanings.
- we need to draw a correspondence map between entities and procedures.
- this means to translate the entity names and,
- to translate their interaction manners.

Lets consider two hospitals with two similar rules:

Rule8: Physicians can manage any medical record.

Rule9: Health Professionals can manage any medical record.

*managing* a medical record includes actions such as *reading*, *writing*, and *signing* one of its entries.

for H' signing and writing a medical record are things completely different and for H'' to sign a medical record is a particular case of writing it.



# FST COMPOSITION FOR POLICY MAPPING

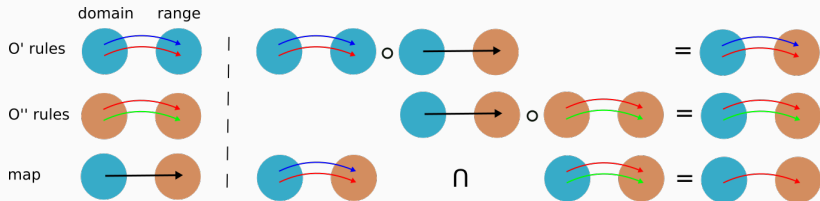


Figure 16: General interoperability analysis process.

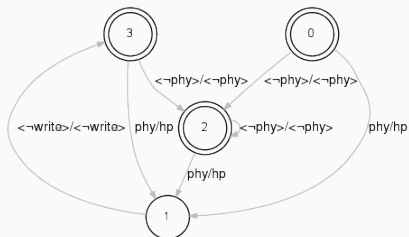


**Figure 17:** FST  $T_{\text{Rule8}}$  modelling Rule 8. The label *phy* represents the set of *physicians*, *man* represents the class of actions *management* and *rec* the class of objects *medical records*.



**Figure 18:** FST  $T_{\text{Rule9}}$  modelling Rule 9. The label *hp* represents the set of subjects *health professionals*, *man* represents the class of actions *management* and *rec* the class of objects *medical records*.

*Physicians* maps to *Health Professionals*, but not when writing a health record.



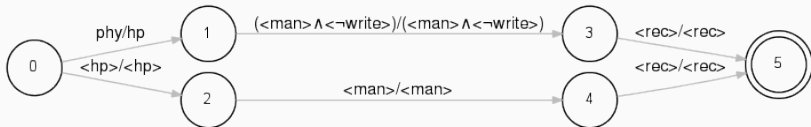
**Figure 19:** FST  $T_{map}$  which defines a map between the entities of two simple permissions.



**Figure 20:** The FST  $T_{R8\_map} = T_{Rule\ 8} \circ T_{map}$ . This models “Physicians can manage any medical record.” with its output actions written in terms of the entities of H” policy.

This computation is based on the presumption that  $read \rightarrow man$ ,  $man \rightarrow \neg rec$ ,  $man \rightarrow \neg phy$ , and  $rec \rightarrow \neg phy$ .

# FST COMPOSITION FOR POLICY MAPPING



**Figure 21:** The FST  $T_{map\_R9} = T_{map} \circ T_{Rule\ 9}$ . This models “*Health Professionals can manage any medicalrecord.*” with its input events written in terms of the entities of H’ policy.

This computation is based on the presumption that  $read \rightarrow man$ ,  
 $man \rightarrow \neg rec$ ,  $man \rightarrow \neg phy$ ,  $man \rightarrow \neg hp$ ,  $rec \rightarrow \neg hp$ ,  $rec \rightarrow \neg phy$ ,  
 $hp \rightarrow \neg phy$ .



**Figure 22:** The  $\tau$ -FST  $T_{p_{int}^+} = T_{R8\_map} \cap T_{map\_R9}$ .  $T_{int}$  is the transducer representing what a subject of  $H'$  can do on  $H''$  objects when the policies of both organization are applied at the same time.

The procedure to find out what are the actions that a subject of a provider  $O'$  can do on the objects of another provider  $O''$ , follows the steps below:

1. to model the policies of organization  $O'$  as the transducer  $T_{O'}$ ,
2. to model the policies of organization  $O''$  as the transducer  $T_{O''}$ ,
3. to model the entity map between  $O'$  and  $O''$  as the transducer  $T_{map}$ ,
4. to compute  $T_{O'_map} = T_{O'} \circ T_{map}$ ,
5. to compute  $T_{map_{O''}} = T_{map} \circ T_{O''}$ , and,
6. to compute  $T_{int} = T_{O'_map} \cap T_{map_{O''}}$

$T_{int}$  is the transducer which models the set of interoperability policy-rules between  $O'$  and  $O''$ .

- We used the extensive FST and Semirings theory to *operate* with policies from different organizations and study their interrelations,
- we are able to compute the security policy that emerges from the combination of all the organization-level policies and,
- the higher-level interoperability policy when two organizations cooperate.
- This work was **partially** described in the paper:  
J. Baliosian and A. Cavalli, “An Abstraction for the Interoperability Analysis of Security Policies”, in proceedings of **NSS 2015**, 9th International Conference on Network and System Security, November 3-5, 2015, New York City, USA.



Further work:

- Writing rules back from FSTs, (made but too many slides)
- integration with Orbac policy manger and MotOrBac policy editor, (started)
- objective-oriented conflict resolution, (to be made)
- Self-Management (control loops for network management systems), (lots made on opportunistic networks, etc.)
- Human-walk modelling. This is starting just now.

# “FREQUENTLY ASKED QUESTIONS”

- Why using FSTs instead of FSRs?
- Why using FST instead of a logic programming approach?
- How weights are selected?
- How do I know that they are right?
- What is new? (your first work with FSTs is from 2004)
- How do I know that the model is complete?
- How do I know that the model is right?

REAL QUESTIONS?

The answer to the third question

**is the emerging policy in line with their cooperation objectives?**

worth a complete research work on itself, but, at least

**we can write policy rules back from its FST model.**

Writing back a set of policies  $P_{int}$  in a high-level specification language such as OrBAC from  $T_{int}$ , is analogous to find

$$\hat{n}_{P_{int}^+} \subseteq \hat{n}_{P_{int}}$$

which corresponds to the permissions  $P_{int}^+$  and

$$\hat{n}_{P_{int}^o} \subseteq \hat{n}_{P_{int}}$$

for the obligations  $P_{int}^o$ .

*(Re-writing the set of prohibitions does not have a meaning in a context where everything that is not permitted is prohibited)*

$\hat{\Pi}_{P_{int}^+}$  is the subset of the relation that maps strings from the language of events  $L_{P^+}$ , where each string has the form “*context, role, activity, view*”, with exactly the same string.

$$T_{P_{int}^+} = id(R_{P^+}) \cap T_{P_{int}}$$

where  $R_{P^+}$  is the FSR that accepts  $L_{P^+}$ .

$\hat{\Pi}_{P_{int}^o}$  is the subset of the relation that maps *activation context* starting events (start\_ac) to strings of the form “*role, activity, view, fulfilled*”, or strings with an *activation context* starting event and a *violation context* starting event (start\_vc) to strings of the form “*role, action, view, fulfilled, violated*”.

$\hat{\Pi}_{P_{int}^o}$  is defined by the FST

$$T_{P_{int}^o} = T_{P^o} \cap T_{P_{int}}$$

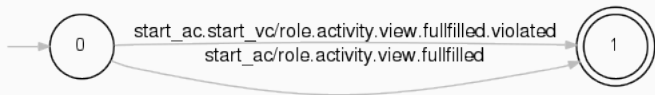


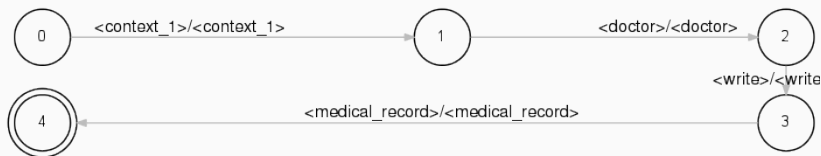
Figure 23: The transducer  $T_{po}$  used to compute  $T_{po_{int}}$

All the FST must be determinised and in its minimal representation.



**Each valid path in  $T_{P_{int}^+}$  corresponds to a permission in  $P_{int}^+$ , and, each valid path in  $T_{P_{int}^o}$  corresponds to an obligation in  $P_{int}^o$ .**

For example, if the path in Figure 51 belongs to  $T_{P_{int}^+}$  the policy `permission(p,doctor,write,medical_record,context_1)` is in the set  $P_{int}^+$ .



belongs to  $T_{P_{int}^+}$ , then, the policy  
`permission(p,doctor,write,medical_record,context_1)`  
is in the set  $P_{int}^+$ .

1. compute  $T_{int}$  (as seen before),
2. compute  $T_{P_{int}^+} = id(R_{P^+}) \cap T_{P_{int}}$ ,
3. compute  $T_{P_{int}^o} = T_{P^o} \cap T_{P_{int}}$ ,
4. find each valid path in  $T_{P_{int}^+}$ ,
5. write a permission for each path using the *context*, *role*, *activity*, and *view* in the path,
6. find each valid path in  $T_{P_{int}^o}$ , and,
7. write an obligation for each path using the *activation context*, *violation context*, *role*, *activity*, and *view* in the path.



J. Baliosian and D. Wonsever, “Finite State Transducers,” in Handbook of Finite State Based Models and Applications, Chapman and Hall/CRC, 2012, pp. 45–68.



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MORE QUESTIONS?